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We would like to dedicate these extended abstracts and references to the doctors, nurses, health workers and all those fighting on the front lines, risking their lives to keep us all safe from the deadly corona virus

We as mathematics educators involving in curriculum studies, have a great and historical responsibility to facilitate and enhance students' learning in this rather strange era! The paradigm shift is happening right in front of our eyes. If we don't use this opportunity to make a better future for our children, the regret will rest upon us forever.

(Celebrating the Establishment of the Doctoral Program of Mathematics Education after 20 Years of its Foundation in the beginning of this millennium: 2000)

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The Necessity of Developing a Qualitative Rubric to Implement the Descriptive Evaluation of Mathematics at the Elementary Schools in Iran

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Extended Abstract

Introduction

More than 15 years has been passed since the Ministry of Education in Iran, launched the “descriptive evaluation” program for elementary schools at the national level. To support the successful implementation of this program that had several pilot studies prior to that, almost all elementary teachers have participated in various in- service training sessions at national, regional and local levels.

Purpose

A number of national assessments indicated that the implementation phase of the “descriptive evaluation” program has not reached the expected level. For this reason, a study was conducted to shed more lights into this issue by investigating more in- depth, the elementary teachers’ ambiguities with the ways in which, the descriptive assessment expected to be implemented according to the formal guideline imposed by the Ministry of Education in Iran.

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Methodology

To serve this purpose, a qualitative study was designed and conducted in which, one 5th Grade class with 27 students along with its teacher, as well as seven other 5th Grade independent teachers, voluntarily participated in that. The data were collected via two mathematics word problems focusing on reasoning and the data were collected through various sources of triangulation and the for the sake assurance the conformability of the data. These sources included classroom teacher's assessment of students, 27 students' portfolios including sample of their activities, solutions to mathematics problems, teacher's observations and other documents related to their mathematics learning. As well, seven independent teachers' assessments and the 1st author's field notes and observations while students were solving problems. The data then, systematically reduced at three different levels; at the first level, 27 individual files were made containing the solutions of each to both problems. At the second level, all solutions to two problems, merged into eight classes according to the variety of reasoning types and finally at the third level, one major category emerged and labeled as "reasoning."

Result

The main result of the study was identification of "principles" for designing a "descriptive rubric". These principles entailed of qualitative vs. quantitative, relative vs. absolute, flexible vs. rigid, content- dependent vs. content- free and based on teachers' judgments supported by the documents and observations collected in students' portfolios as opposed to being objective.

Discussion

The study came to the conclusion that the successful implementation of any kind of descriptive evaluation programs, requires knowledgeable and independent teachers with relatively high self-esteem who believe on the effectiveness of descriptive evaluation for the enhancement of teaching- learning process, to some degree. Further, elementary teachers need to be supported by the education authority not just being told what to do in training sessions, but also their judgments and decisions be reinforced by them, regarding students' performance. Last not the least, is to clearly hear elementary



teachers' unheard voices that the learning at any level, is reciprocal and interactive. No teacher could silently sit hours and hours in a training session to be dictated guidelines that he/ she has not been part of it. Instead, teachers should be considered as the major stakeholder for implementing any education change- no matter small or large scale.

Keywords: Descriptive Evaluation Program, Qualitative Rubric, Elementary Teachers, Mathematics Content, Grade 5 Students.

References

- Anderson, R. S., & Puckett, J. B. (2003). Assessing students' problem-solving assignments. *New Directions for Teaching and Learning*, (95), 81-87. <http://dx.doi.org/10.1002/tl.117>.
- Assessment Reform Group. (2002). Assessment for learning: 10 principles. Available at www.assessment-reform-group.org.
- Bennett, R. E. (2011). Formative assessment: A critical review. *Assessment in Education: Principles, Policy & Practice*, 18(1), 5–25. doi:10.1080/0969594X.2010.513678.
- Black, P. Harrison, C. Lee, C., Marshall, B., and William, D. (2004). Working inside the box: Assessment for Learning in the classroom. *Phi Delta Kappan*. 86 (1), 8-21.
- Black, P., & William, D. (2009). Developing the theory of formative assessment. *Educational Assessment, Evaluation and Accountability*, 21 (1), 5–31.
- Bleiler, S. K., & Thompson, D. R. (2013). Multi-dimensional assessment of the common core. *Teaching Children Mathematics*, 19(5), 292–300.
- Brookhart, S. M. (2003). Developing measurement theory for classroom assessment purposes and uses. *Educational Measurement: Issues and Practice*, 22(4), 5–12.
- Brookhart, S. M. (2013). How to create and use rubrics for formative assessment and grading. Alexandria,VA: Ascd.
- Burns, M. (2007). *About teaching mathematics: A K-8 resource* (3rd Ed.). Sausalito, CA: Math Solutions.

- De Lange, J. (2007). Large-scale assessment and mathematics education. In F. K. Lester, Jr. (Ed.), *Second handbook of research on mathematics teaching and learning* (pp. 1111–1142). Charlotte, NC: Information Age Publishing.
- De Luca, C., & Volante, L. (2016). Assessment for learning in teacher education programs: Navigating the juxtaposition of theory and praxis. *Journal of the International Society for Teacher Education*, 20(1), 19–31.
- Fan, L. (2011). Implementing self-assessment to develop reflective teaching and learning in mathematics. In B. Kaur & K. Y. Wong (Eds.), *Assessment in the mathematics classroom: 2011 Association of Mathematics Educators Yearbook* (pp. 275–290). Singapore: World Scientific Publishing.
- Gardner, J. (2012). Assessment for learning: Introduction. In J. Gardner (Ed.), *Assessment and Learning* (2nd ed., pp. 1–8). London: Sage.
- Gholamazad, S. (2011). Mathematics Assessment. *Roshd Mathematics Education Journal*. No. 105, 14- 18. Publication & Teaching Technology Office, Organization for Research & Educational Planning, Ministry of Education. (In Farsi.)
- Hassani, M., & Pozesh Shirazi, H. (2014). An Analysis of the Researches Concerning the Descriptive Qualitative Evaluation. *Journal of Education and Psychology*. 21(1); 21- 50. Shahid Chamran University. (In Farsi.)
- Hattie, J. A. C., & Timperley, H. (2007). The power of feedback. *Review of Educational Research*, 77(1), 81–112. Doi: 10.3102/003465430298487.
- Kulm, G. (1994). *Mathematics assessment: What works in the classroom?* San Francisco, CA: Jossey Bass Inc.
- Li, M., Yin, Y., Ruiz-Primo, M. A., & Morozov, A. (2011). *Identifying effective feedback practices on student mathematics learning: A literature synthesis*. Paper presented at the meeting of American Educational Research Association, New Orleans, LA.
- Lund, A. (2008). Assessment made visible: Individual and collective practices. *Mind, Culture, and Activity*, 15, 32–51.



- McTighe, J. (2015). What is a performance task? Retrieved from <http://www.performancetask.com>.
- Moss, C. M., & Brookhart, S. M. (2009). *Advancing formative assessment in every classroom: A guide for instructional leaders*. Alexandria, VA: ASCD.
- National Council of Teachers of Mathematics (NCTM). (2014). *Principles to action: Ensuring mathematical success for all*. Reston, VA: The Author.
- Newton, P. E. (2007). Clarifying the purposes of educational assessment. *Assessment in Education: Principles, Policy and Practice*, 14(2), 149-170.
- Ontario Ministry of Education. (2010). *Growing success: Assessment, evaluation, and reporting in Ontario schools*. Retrieved from <http://www.edu.gov.on.ca/eng/policyfunding/growSuccess.pdf>
- Sato, M., Wei, R. C., & Darling-Hammond, L. (2008). Improving teachers' assessment practices through professional development: The case of National Board Certification. *American Educational Research Journal*, 45(3), 669–700. Doi: 10.3102/0002831208316955.
- Regulations for evaluating the educational and training progress of the primary school. (2008). Resolution 769 of the Commission on Statutes and Academic Regulations of the Higher Education Council on 4/18/2008. Retrieved from the Higher Education Council Portal; <https://www.medu.ir/fa/>
- Stenmark, J. K. (1991). (Ed.); *Mathematics Assessment: Myths, Models, Good Questions and Practical Suggestions*. The National Council of Teachers of Mathematics, Reston, VA. (Translated into Farsi by A. Gooya & M. Rezaie, 2008, with author's permission- 1387 Solar year, Fatemi Publishing House, Tehran, Iran.)
- Suurtamm, C., & Koch, M. J. (2014). Navigating dilemmas in transforming assessment practices: Experiences of mathematics teachers in Ontario, Canada. *Educational Assessment, Evaluation and Accountability*, 26(3), 263–287.
- Toh, T. L., Quek, K. S., Leong, Y. H., Dindyal, J., & Tay, E. G. (2011). Assessing problem solving in the mathematics curriculum: A new approach. In B. Kaur & K.

- Van de Walle, J. A., Karp, K. S., & Bay-Williams, J. M. (2009). *Elementary and middle school mathematics: Teaching developmentally* (7th Ed.). Boston, MA: Allyn & Bacon/Merrill.
- Watt, H. (2005). Attitudes to the use of alternative assessment methods in mathematics: A study with secondary mathematics teachers in Sydney, Australia. *Educational Studies in Mathematics*, 58(1), 21-44.
- William, D., Lee, C., Harrison, C., & Black, P. (2004). Teachers developing assessment for learning: Impact on Student achievement. *Assessment in Education*, 11 (1), 49 - 64.
- William, D. (2011). What is assessment for learning? *Studies in Educational Evaluation*, 37(1), 3–14. doi:10.1016/j.stueduc.2011.03.001
- William, D., & Thompson, M. (2007). Integrating assessment with instruction: what will it take to make it work? In C. A. Dwyer (Ed.). *The future of assessment: shaping teaching and learning* (pp. 53-82). Mahwah, NJ: Lawrence Erlbaum Associates.
- Wilson, S. M., & Kenney, P. A. (2003). Classroom and large-scale assessment. In J. Kilpatrick,
- Wylie, E. C., & Lyon, C. J. (2015). The fidelity of formative assessment implementation: Issues of breadth and quality. *Assessment in Education: Principles, Policy & Practice*, 22(1), 140–160. doi:10.1080/0969594X.2014.990416.



Developing a Model based on Constructivism Approach, for Teaching Simplification of Algebraic Expressions in the 8th Grade

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Extended Abstract

Introduction

Mathematics, due to its nature, has a special role and place in school mathematics curriculum and its teaching and learning has always been one of the great concerns of educational systems in the world. However, the world needs competent people more than ever, to use mathematics for modelling real world phenomena and finding suitable solutions for them.

Purpose

The aim of the present study was developing a model taking constructivism approach, for teaching simplification of algebraic expressions in the 8th Grade.

Methodology

The study conducted at two phases, and according to its purpose, mixed research methodology was chosen. At the first phase, a model was developed and a focus group was formed consisting of 15 volunteer mathematics teachers of the same grade. They met three times until the model was modified and validated for implementation. At the second phase, an experimental study was designed involving 60 Grade 8 students that randomly selected and assigned to two experimental and control groups. After administering a pre-test, both groups were taught by the first author whom, is mathematics teacher for 11 years and has taught the Grade 8 national mathematics textbook

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accordingly. The control group was taught as usual and the experimental group was taught using the developed model as treatment. At the end of the teaching the simplification of algebraic expressions, a post- test was carried out for both groups to see the effect of the treatment; i.e. the developed model. For the analysis of the data collected from post- test, a Co-variance test was conducted.

Results

The results showed that the difference between the two groups' scores was statistically significant in the favor of the experimental group. This indicated the effectiveness of the developed model on students' performance on simplification of algebraic expressions.

Discussion

Teaching models have proved to be effective in enhancing students' performances in mathematics. Therefore, by explaining and implementing educational models based on the constructivism approach, students' mathematics learning was improved. Educational models based on constructivism, inspire students to think and encourage them to cooperate and interact with each other while solving problems and enhance their mathematics learning. As well, students engaged in the process of constructing their own knowledge of algebraic expressions, which is the chief principle of the constructivism approach. The concluding remark of this research study is that mathematics teachers need all kinds of educational support for designing, developing and implementing mathematics teaching models to enhance students' mathematics learning, using constructivism approach.

Keywords: Constructivism, Simplification of Algebraic Expressions, Mixed Method, 8th Grade Students.



References

- Baker, W., Czarnocha, B., & Prabhu, V. (2004). Procedural and conceptual knowledge in mathematics. *Proceedings of the North American Chapter of the International Group for the Psychology of Mathematics Education*. Toronto, Ontario, Canada.
- Beyrami poor, A., & Liaqat dar, M. J. (2009). Quality of teaching of mathematics of fourth grade in Isfahan in order to provide strategies for improving student performance in international tests Thames. *Journal of Education*, 25 (4), 49-68. (In Farsi.)
- Booker, G. (1987). Conceptual obstacles to the development of algebraic thinking. In J. Bergeron, N. Herscovics & C. Kieran (Eds.). *Proceedings of the eleventh international conference Psychology of Mathematics Education* (Vol. 1, pp. 275-281). Montreal: PME.
- Bush, S. B. (2011). *Analyzing common algebra-related misconceptions and errors of middle school students* (Doctoral dissertation). Retrieved from <https://doi.org/10.18297/etd/187>.
- Capraro, M. M. & Joffrion, H. (2006). Algebraic equations: Can middle-school students meaningfully translate from words to mathematical symbols? *Journal of Reading Psychology*, 27 (1), 147-164. Doi: 10.1080/027027106006442467.
- Cavallo, A.M.L., & Laubach, T.A. (2001). Students' science Perceptions and Enrollment Decisions in Differing Learning Cycle Classrooms. *Journal of Research in science Teaching*, 38(9):1029-1062.
- Dekock, A., Sleepers, P., & Voeten, JM. (2004). New Learning and the Classification of Learning Environments in Secondary Education. *Review of Educational Research*. 74 (2). 141-170.
- Doerr, H. (2004). Teacher's knowledge and the teaching of algebra. In K. Stacey, H. Chick & Kendal (Eds.), *The Future of Teaching and Learning of algebra. The 12th ICMI Study* (pp. 267-290). Boston: Kluwer.
- Dogru, A. P. and Tekkaya, C. (2008). Promoting Students Learning in Genetics with the Lesrning Cycle. *Journal of Experimental Education*, 76 (3).
- Driscoll, M. (2000). *Psychology of Learning for instruction*. Needham Heights, MA, Allyn & Bacon.

- Fleisch, B. (2008). *Primary education in crisis: Why South African Schoolchildren underachieve in reading and mathematics*. Juta Academic: Cape Town, South Africa. Retrieved from <http://www.amazon.co.uk>.
- Folger, E. (2005). *Efficacy of mastery learning as a method of instruction: implications for instructional leaders* (Doctoral desertation). Ashland, Ashland University.
- Frid, S. (2000). Using learning cycle in mathematics: more than the sum of parts. *Australian Mathematics teacher*, 56 (4): 32-37.
- Guler, M. & Celic, D. (2016). A research on future mathematics teacher's instructional explanations: the case of algebra. *Journal of Educational Research and Reviews*. 11(16), 1500-1508. 10.5897/ERR2016.2823.
- Hakkarainen, A., Holopainen, L., & Savolainen, H. (2013). Mathematical and reading difficulties as predictors of school achievement and transition to secondary education. *Scandinavian Journal of educational research*, 57(5): 488-506.
- Jacobse, A. E., & Harskamp, E. G. (2012). Toward efficient measurement of metacognition in mathematical problem solving. *Metacognition and Learning*, 7 (2): 133-149.
- Jia, Q. (2010). A /brief Study on the Implication of Constructivism Teaching Theory on Classroom Teaching Reform in Basic Education. *International Education Studies*, 3 (2): 197-199.
- Jordan, N. C., & Levine, S. C. (2009). Socioeconomic variation, number competence, and mathematics learning difficulties in young children. *Developmental Disabilities Research Reviews*, 15 (1): 60-68.
- Kaput, J. (2008). What is algebra? What is algebraic reasoning? In J.J. kaput, D. W. Carraher & M. L. Blanton (Eds.), *Algebra in the early grades* (pp. 5-18). New York: Taylor & Francis Group & National Council of Teachers of Mathematics.
- Lacroix, L.N. (1991). *Mathematics Teaching Practice: A Constructivist Perseptive* (Unpublshed manuscript), the University of British Columbia, Canada.
- Lebow, D. (1993). Constructivist Values of Instructional System Design: Five Principles toward a new Mindset. *Educational Technology Research & Development (ETR&D)*, 41 (3). 4-16.



- MacGregor, M. (2004). Goals and Content of an algebra curriculum for the compulsory years of schooling. In K. Stacey, H. Chick & Kendal (Eds.), *The Future of Teaching and Learning of algebra: The 12th ICMI Study* (pp. 313-328). Boston: Kluwer.
- Mamba, A. (2012). *Learner's errors when solving algebraic tasks: A case study of grade 12 mathematics examination papers in South Africa* (Unpublished doctoral dissertation). Johannesburg University, South Africa.
- Mest, O. (2006). *The effect of (7E) learning cycle model on Improvement of fifth grade students' critical thinking skills*. A thesis submitted to the graduate school of natural land applied sciences of Middle East Technical University.
- Norton, S. & Irwin, J. (2007). A concrete approach to teaching algebra. In J. M. Watson & K. Beswick (Eds.), *Proceedings of the 30th annual conference of the Mathematics Education Research Group of Australasia*. (pp. 561-570). Hobart, Sydney: MERGA.
- Novello, A. C., Degraw, C., & Kleinman, D. (2007). Healthy children ready to learn: An essential collaboration between health and education. *Public Healthy Reports*, 107: 3-15.
- Odom, A.L., & Kelly, P.V. (2001). Integrating Concept Mapping and the Learning Cycle to Teach Diffusion and Osmosis Concepts to High School Biology Students. *Science Education*, 85, 615-635.
- Olsen, DG. (2000). Constructivist principles of Learning and Teaching Methods. *Education*. 120 (2). 347-355.
- Olusegun, B.S. (2015). Constructivism Learning Theory: A Paradigm for Teaching and Learning. *IOSR Journal of Research & Method in Education*, 5(6): 66-70. Doi: 10.9790/7388-05616670
- Owusu, J. (2015). *The Impact of Constructivist- Based Training method on Secondary School Learners Errors in Algebra* (Master dissertation). Retrieved from <http://hdl.handle.net/10500/19207>.
- Polya, G. (1945). *How to solve it*. Princeton University Press. Princeton science library.
- Reyna, V. F., & Brainerd. C. J. (2007). The importance of mathematics in health and human judgment: Numeracy, risk communication, and medical decision making. *Learning and Individual Differences*, 17(2):147-159.
- Richard, J. C. (1996). *Turning to the artistic: developing an enlightened eye by greating teaching self-portraits*. Paper

- presented at the international conference, Herstmonceux castle, East Sussex, England, August 5-8.
- Seng, L. K. (2010). An error analysis of Form 2 (Grade 7) students in simplifying algebraic expressions: A descriptive study. *Electronic Journal of Research in Education Psychology*, 8(1): 139-162.
- Shoenfeld, A.H. (1995). *Cognitive Science and Mathematics Education Overview*.
- Shulman, L.S. (1986). Those who understand: knowledge growth in teaching. *Journal of Educational researcher*, 15 (2), 4-14. Doi: 10.3102/0013189X015002004.
- Thompson, S. A., & Tilden, V. P. (2009). Embracing quality and safety education for the 21st century: building inter professional education. *Journal of Nursing Education*, 48: 698-701.
- Usiskin, Z. (1995). Why is algebra important to learn? *American Educator*, 30-37.
- Woolley, N. N., Jarvis, Y. (2007). Situated cognition and cognitive apprenticeship: A model for teaching and learning clinical skills in a technologically rich and authentic learning environment. *Nurse Educ Today*, 27(1): 73-9.



Influencing Factors and Relationships between them to enhance the Usage of Digital Technologies by Primary and Mathematics Teachers

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Extended Abstract

Introduction

Integrating digital technologies in teaching and learning processes is a universal phenomenon which is often recommended by governments, universities, education faculties, and schools in order to improve educational systems. Despite the capabilities of digital tools, their usage is new in classrooms and restricted to primary grades.

Purpose

The present study was conducted with an exploratory sequential mixed method approach in two steps to extract influential factors that enhance the use of digital technologies in the courses such as mathematics which student achievements based on international exam are less than average score.

Methodology

To do so, in the first step, semi-structured interviews were conducted with six groups of from 3 to 5 primary and mathematics high school teachers, respectively. These informants were selected purposefully according to accessibility level to digital technologies and teachers' skills to use them. In addition, influencing factors were extracted, through a quantitative approach, survey method participating 457 people using path analysis, and the relationships amongst factors were examined, and several recommendations were proposed. Validity and

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reliability were improved through the Rasch-Andrich measurement model. Additionally, structural equation modeling also was applied to examine construct validity as well.

Results

Some themes were extracted in the first step of the study, such as lack of hardware and software infrastructures, in-service education, technical support, and lack of situations in textbooks to use digital tools and a high volume of textbooks. Students' use of digital tools and teachers' sharing experiences of using digital technologies, teachers' beliefs, and the principals' roles and importance of the schools were some other themes as well. Next, using a quantitative approach, a survey using a questionnaire was conducted to investigate the construct validity and the relationships between the latent factors. Exploratory factor analysis showed factors which named school importance, availability, and collaboration, students' use of digital tools, teacher's beliefs, and skills. School readiness contributed to teacher readiness, and these two had a statistical significant effect on student's use of digital technologies.

Discussion

Findings are applicable in integrating digital technologies in textbooks and teacher education programs as well. Providing technical supports, along with the promotion of the teachers' skill to work with digital technologies, are suggested to facilitate integrating digital technologies in teaching and learning processes, particularly in mathematics education. Digital technologies can be used for more than provision and support of traditional teaching and learning methods. Not only should teachers learn to use digital tools to promote traditional teaching models, but also they should learn how digital technologies can be integrated into teaching and learning to enhance a student-centered perspective.

Keywords: Digital technologies, Upper primary School, Primary Teachers, Junior Secondary Mathematics Teachers.



References

- Alagic, M. (2003). Technology in the mathematics classroom: Conceptual orientation. *Journal of Computers in Mathematics and Science Teaching*, 22(4), 381-399.
- Badia, A., Meneses, J., Sigalés, C., & Fàbregues, S. (2014). Factors affecting school teachers' perceptions of the instructional benefits of digital technology. *Procedia – Social and Behavioral Sciences*, 141, 357–362.
- Beauchamp, G. & Parkinson, J. (2008). Pupils' Attitudes towards School Science as they Transfer from an ICT-rich Primary School to a Secondary School with Fewer ICT Resources: Does ICT Matter? *Educ Inf Technol*, 13(2), 103–118.
- Blundell, C. N. (2017). *A case study of teachers transforming pedagogical practices through collaborative inquiry-based professional learning in a ubiquitous technologies environment* (Doctoral dissertation, Queensland University of Technology). Retrieved from https://eprints.qut.edu.au/112463/1/Christopher_Blundell_Thesis.pdf
- Blundell, C., Lee, K. T., & Nykvist, S. (2019). Using Dual Systems theory to conceptualise challenges to routine when transforming pedagogy with digital technologies. *Teachers and Teaching*, 25(8), 937-954.
- Blundell, C., Lee, K. T., & Nykvist, S. (2020). Moving beyond enhancing pedagogies with digital technologies: Frames of reference, habits of mind and transformative learning. *Journal of Research on Technology in Education*, 52(2), 178-196.
- Bowers, J. S., & Stephens, B. (2011). Using technology to explore mathematical relationships: A framework for orienting mathematics courses for prospective teachers. *Journal of Mathematics Teacher Education*, 14(4), 285–304.
- Cheung, A. C. K., & Slavin, R. E. (2013). The effectiveness of educational technology applications for enhancing mathematics achievement in K–12 classrooms: A meta-analysis. *Educational Research Review*, 9, 88–113.

- Creswell, J. (2009). *Research design: Qualitative, quantitative, and mixed methods approaches* (3rd ed.). London, England: Sage Publications.
- Daly, C., Pachler, N., & Pelletier, C. (2009, May). *Continuing professional development in ICT for teachers: A literature review*. WLE Centre, Institute of Education, University of London, England: BECTA.
- Drijvers, P. (2018). Empirical evidence for benefit? Reviewing quantitative research on the use of digital tools in mathematics education. In L. Ball, P. Drijvers, S. Ladel, H.-S. Siller, M. Tabach, & C. Vale (Eds.), *Uses of technology in primary and secondary mathematics education; tools, topics and trends* (pp. 161–178). Cham: Springer International Publishing.
- Ertmer, P. A. (2015). Technology integration. In J. M. Spector (Ed.), *The SAGE encyclopedia of educational technology* (pp. 748–751). Thousand Oaks, CA: Sage.
- Fu, J. S. (2013). ICT in education: A critical literature review and its implications. *International Journal of Education and Development using Information and Communication Technology*, 9(1), 112-125.
- Galbraith, P., Stillman, G., Brown, J., & Edwards, I. (2007). Facilitating middle secondary modelling competencies. In C. Haines, P., Galbraith, W., Blum, & S. Khan, (Eds.), *Mathematical modelling: Education, engineering and economics* (pp. 130-140). Chichester, UK: Horwood.
- Hair, J., Black, W., Babin, B., & Anderson, R. (2010). *Multivariate data analysis* (7th Ed.); Upper Saddle River, NJ, USA: Prentice-Hall, Inc.
- Han, I., Byun, S. Y., & Shin, W. S. (2018). A comparative study of factors associated with technology-enabled learning between the United States and South Korea. *Educational Technology Research and Development*, 66(5), 1303-1320.
- Hosseini, Z. (2015). The Comparison between the Effect of Constructivism and Directed Instruction on Student Teachers' Technology Integration. *New educational approaches*, 10(2), 14-24. (In Persian)
- Hoyles, C. (2018). Transforming the mathematical practices of learners and teachers through digital technology. *Research in Mathematics Education*, 20(3), 209-228.



- Hsu, S., & Kuan, P.-Y. (2013). The impact of multilevel factors on technology integration: the case of Taiwanese grade 1–9 teachers and schools. *Educational Technology Research and Development*, 61(1), 25–50.
- Khalid, M. S., & Nyvang, T. (2014). A change agent's facilitation process for overcoming the barriers of ICT adoption for educational administration: The case of a rural-Bangladesh vocational institution. *Australasian Journal of Educational Technology*, 30(5), 547-561.
- Khorooshi, P. Nasr Esfahani, A.R. & Mirshah Jafary, E. (2018). The Conceptual Model of Evaluation of Expected Competences of the Teacher-Students in Competency-based Teacher Training Curriculum, *Journal of curriculum studies*, 13(50), 5-44. (In Persian)
- Landis, J. R., & Koch, G. G. (1977). The measurement of observer agreement for categorical data. *Biometrics*, 33(1), 159-174.
- Lee, C.Y., & Chen, M. J (2016). Influence of Prior Knowledge and Teaching Approaches Integrating Non-routine Worked Examples and Digital technologies on the Performance and Attitude of Fifth-Graders in Learning Equivalent Fractions. In P. S. Moyer-Packenham (Ed.), *International Perspectives on Teaching and Learning Mathematics with Virtual Manipulatives* (pp. 189-212). Cham, Switzerland: Springer.
- Li, Q., & Ma, X. (2010). A meta-analysis of the effects of computer technology on school students' mathematics learning. *Educational Psychology Review*, 22(3), 215–243.
- Lindsay, L. (2016). Transformation of teacher practice using mobile technology with one-to-one classes: M-learning pedagogical approaches. *British Journal of Educational Technology*, 47(5), 883-892.
- Liu, F., Ritzhaupt, A. D., Dawson, K., & Barron, A. E. (2016). Explaining technology integration in K-12 classrooms: A multilevel path analysis model. *Educational Technology Research and Development*, 65(4), 795–813.
- Mahdavi, M., Malaki, H., Mehrmohammadi, M., & Abbaspour, A. (2016). A comparative study on the teacher education curriculums at the elementary levels based on the competency-based approach

- in Malaysia, India and Iran. *Journal of curriculum studies*, **11(41)**, 23-64. (In Persian)
- Makki, T. W., O'Neal, L. J., Cotten, S. R., & Rikard, R. V. (2018). When first-order barriers are high: A comparison of second- and third-order barriers to classroom computing integration. *Computers & Education*, *120*, 90-97.
- Martin, M. O., Mullis, I. V. S., & Hooper, M. (Eds.). (2016). *Methods and Procedures in TIMSS 2015*. Retrieved from Boston College, TIMSS & PIRLS International Study Center website: <http://timssandpirls.bc.edu/publications/timss/2015-methods.html>
- Mishra, P., & Koehler, M. (2006). Technological pedagogical content knowledge: A framework for teacher knowledge. *Teachers College Record*, *108(6)*, 1017–1054.
- National Council of Teachers of Mathematics. (2000). *Principles and standards for school mathematics*. Reston, VA: Author.
- Nielsen, W., Miller, A., & Hoban, G. F. (2012). *The digital education revolution: New South Wales science teachers' response to laptop ubiquity*. *AERA Annual Meeting 2012*. Retrieved from <http://ro.uow.edu.au/edupapers/1086/>.
- Petko, D., Prasse, D., & Cantieni, A. (2018). The Interplay of School Readiness and Teacher Readiness for Educational Technology Integration: A Structural Equation Model. *Computers in the Schools*, *35(1)*, 1-18.
- Puentedura, R. (2014). *SAMR in the classroom*. Retrieved from <http://www.hippasus.com/rrpweblog/archives/2014/08/27/SAMRInTheClassroom.pdf>
- Robová, J. (2013). Specific skills necessary to work with some ICT tools in mathematics effectively. *Acta Didactica Mathematicae*, *35*, 71–104.
- Rogers, E. M. (2003). *Diffusion of innovations* (5th ed.). New York: Free Press.
- Seraji, F. and Soleymani, F. (2016). Analysis of ICT integration (cyber spacing) obstacles at implementation stage based on educational innovation theories in schools. *Journal of Curriculum Studies*, *11(42)*, 153-176. (In Persian)
- Shulman, L. S. (1987). Knowledge and teaching: Foundations of the new reform. *Harvard Educational Review*, *57(1)*, 1- 22.



- Sokolowski, A., Li, Y., & Willson, V. (2015). The effects of using exploratory computerized environments in grades 1–8 mathematics: A meta-analysis of research. *International Journal of STEM Education*, 2(1), 1–17.
- Tarhini, A., Arachchilage, N.A.G., Masa'deh, R., & Abbasi, M.S. (2015). A critical review of theories and models of technology adoption and acceptance in information system research. *International Journal of Technology Diffusion*, 6(4), 1–20.
- Thomas, M.O.J. & Palmer, J.M. (2014). Teaching with digital technology: obstacles and opportunities. In A. Clark-Wilson, O. Robutti & N. Sinclair (Eds.), *The Mathematics Teacher in the Digital Era. An International Perspective on Technology Focused Professional Development* (pp. 71-89). Dordrecht: Springer.
- Tondeur, J., Van Braak, J., Ertmer, P. A., & Ottenbreit-Leftwich, A. (2016). Understanding the relationship between teachers' pedagogical beliefs and technology use in education: a systematic review of qualitative evidence. *Educational Technology Research and Development*, 65(3), 555-575.
- Trgalová, J., & Jahn, A. P. (2013). Quality issue in the design and use of resources by mathematics teachers. *ZDM – Mathematics Education*, 45(7), 973–986
- Tunjera, N., & Chigona, A. (2020). Teacher Educators' appropriation of TPACK-SAMR models for 21st century pre-service teacher preparation. *International Journal of Information and Communication Technology Education (IJICTE)*, 16(3), 1–15. DOI: 10.4018/IJICTE.2020070110.
- Uslu, O. (2018). Factors associated with technology integration to improve instructional abilities: A path model. *Australian Journal of Teacher Education*, 43(4), 31-50.
- Zeynivandnezhad, F. & Rashed. F. (2014). *Testing Research Hypotheses Using Structural Equations Modeling*. Tehran: Jame-e-Shenasan. (In Persian)
- Zeynivandnezhad, F. (2018). Validation Instrument to Evaluate Students' Perception of Virtual Manipulatives in Learning Mathematics. *Journal of applied measurement*, 19(4), 387-412.
- Zeynivandnezhad, F., & Bates, R. (2018). Explicating mathematical thinking in differential equations using a computer algebra system.

International Journal of Mathematical Education in Science and Technology, 49(5), 680-704.

- Zeynivandnezhad, F., Mousavi, A., & Kotabe, H. (2020). The Mediating effect of Mathematics Study Approaches on the Relationship between Mathematics Conception and Experiences of Digital Technologies. *Computers in the Schools: Interdisciplinary Journal of Practice, Theory, and Applied Research*. <https://doi.org/10.1080/07380569.2020.1793050> .
- Zhang, Y., & Wildemuth, B. M. (2009). Qualitative analysis of content. In B. Wildemuth (Ed.), *Applications of Social Research Methods to Questions in Information and Library Science* (pp.308-319). Westport, CT: Libraries Unlimited.
- Zheng, B., Warschauer, M., Lin, C.-H., & Chang, C. (2016). Learning in one-to-one laptop environments. *Review of Educational Research*, 86(4), 1052-1084.



Changing School Mathematics Curriculum: Challenges and Required Research

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Extended Abstract

Introduction

In the recent decades, school mathematics curriculum reforms have taken place in many countries. Although the contexts of these reforms differ significantly, research could reveal much informative facts about them. For instance, there is a tendency for many countries to include curriculum standards of developed countries in their national curricula. Due to the special role and nature of mathematics, this tendency can be seen even more in this subject. This phenomenon has become a driving force towards an international curriculum. As result, it is expected mathematical literacy of students across the countries does not differs dramatically, which can be consider as a positive aspect. However, we cannot ignore the negative aspects of this adoption as well.

Purpose

In this regard, and in order to create a change in the Iranian education system, in the last decade, we have witnessed radical and comprehensive changes in terms of structure, content and implementation at the macro level of the Iranian education system. The experience of the last decade shows implementing these changes caused major challenges to the education system in Iran. Given the breadth and complexity of the debates surrounding these challenges, in this article we just focus on the changes in the content of the school mathematics curriculum and, its required research.

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Methodology

For this purpose, after making a distinction between curriculum change and curriculum reform, the influential factors on school mathematics curriculum reforms since the second half of the 20th century onward, and the challenges which have been caused by them have been reviewed.

Results

In recent years, also, the internationalization and globalization of the economy, universality of technological development and related needs for new skills and knowledge play the role of strong historical motivations for curriculum reforms that bring calls for unified standards for mathematics in school. Studies, however, show that the one of the main reasons for the challenges is the neglect of the social and cultural conditions of the countries in the processes of developing their school mathematics curriculum. For example, East West differences in mathematics curricula and reforms which have gained less interest, from the result of international studies such as TIMSS and PISA.

Discussion

Curriculum as a changing agent in an educational reform, plays a significant role in mathematics education. Because it has to determine what students learn, when they learn it, and how they will learn it. Therefore any reform required research to provide clear answer for questions, such as, what aspects of the curriculum should be changed?, how might a curriculum be improved to meet the needs for ever-changing world?, how can educators ensure that the development of students' conceptual understanding does not come at the expense of the development of basic mathematical skills? Or can students learn algorithms and master basic skills as they engage in explorations of mathematically intriguing problems? These are some of the fundamental questions that mathematics educators need to consider in curriculum development and research.

Key words: curriculum change, curriculum reform, school mathematics curriculum.



References

- Ahtiainen, Raisa. (2017). *Shades of change in Fullan's and Hargreaves's models: Theoretical change perspectives regarding Finnish special education reform*. Unpublished Doctoral Dissertation.
- Cai, J. & Howson, G. (2013). Toward an International Mathematics Curriculum. In M. A. (Ken) Clements; A. Bishop; C. Keitel; J. Kilpatrick & F. Leung. (Eds.) *Third International Handbook of Mathematics Education*. Springer.
- Clarkson, P.C., Fitzsimons, G.E., & Seah, W.T. (1999). Values Relevant to Mathematics? I'd like to see that! In D. Tynan, N. Scott, K. Stacey, G. Asp, J. Dowsey, H. Hollingsworth & B. McCrae (Eds.); *Mathematics: Across the ages*. Melbourne: Mathematics Association of Victoria.
- Fullan, M. (2007). *The new meaning of educational change*. New York: Teachers College Press
- Gholamazad, S. (2006): Pre-service Elementary School Teachers' Experiences with Interpreting and Creating Proofs. Unpublished Doctoral Dissertation, Simon Fraser University, Canada.
- Gholamazad, S. (2014). The Trace of Realistic Mathematics Education in the School mathematics in Iran. *Journal of the Theory & Practice in Curriculum*. 2 (3); 47-70. (In Farsi.)
- Gholamazad, S. (2020). Mathematics curriculum evaluation in the first cycle of elementary education (grades 1-3). Unpublished National research report. Organization for Educational Research and Planning (OERP). (In Farsi.)
- Gooya, Z. (2018). Fullan as an Architect and Theorist of Educational Change. Iranian Encyclopedia of Curriculum. Electronic Version. (In Farsi.)
- Gooya, Z., & Gholamazad, S. (2019). Hundred Years of Official Teacher Training Efforts in Iran Starting with the Central Darolmo'allemin. *Quarterly Journal of Education*. 35 (2): 39-60. (In Farsi.)
- Howson, G., & Wilson, B. (1986). *School mathematics in the 1990s*. Cambridge, UK: Cambridge University Press.

- ICMI Study 24. (2017). *School mathematics curriculum reforms: challenges, changes and opportunities*. Tsukuba, Japan.
- Iranmanesh, A., et al. (2010). Mathematics curriculum guide (1-12). Bureau of Compiling Primary and Theoretical Secondary Textbooks. Organization for Educational Research and Planning (OERP). (In Farsi.)
- Kabiri, M. (2013). Evaluation of second and sixth grade mathematics textbooks. National research report. Organization for Educational Research and Planning (OERP). (In Farsi.)
- Leung, F. K. S. (2006). Mathematics education in East Asia and the West: Does culture matter? In F. K. S. Leung, K. D. Graf, & F. J. Lopez-Real (Eds.) *Mathematics education in different cultural traditions: A comparative study of East Asia and the West, the 13th ICMI Study* (pp. 21–46). New York: Springer. Google Scholar.
- Ministry of Science, Research and Technology. (2015). Undergraduates Mathematics Education Curriculum, Farhangian University. (In Farsi.)
- Mortazavi, M., Gooya, Z., Maleki, H., Gholamazad, S. (2020), Challenges of Implementing Descriptive Evaluation of Mathematics in Elementary School in Iran from Teachers Perspective. *Theory & Practice in Curriculum Journal*. Kharazmi University. Iran. (In Farsi.)
- Nieveen, N. & Plomp, T. (2017). *Five Key principle for educational change*. SLO, Enschede. The Netherlands.
- Obanya, P. (2008). Reforming Educational Reforms. Lawal, A.R et. Al. (Eds.) *Educational Reforms in Nigeria*. Faculty of Education, University of Ilorin, 24-46.
- Obanya, P. (2012). Educational change versus educational reform. In Ivowi, UMO and Akpan, Ben B. (Eds.); *Education in Nigeria: From the Beginning to the Future*. Lagos,;Foremost Educational Services Ltd. 441-460.
- OECD. (2003). *The PISA 2003 Assessment Framework-Mathematics, Reading, Science and Problem Solving Knowledge and Skills*. (OECD.org.)
- Rafiepour, A. (2014). Reactions after “New Math”. Farhang va Andishe-ye Riyazi. Vol 54. 1-11. Iranian MathematicAL Society: AMS. (In Farsi.)



- Reys, B. J., Reys, R. E., & Rubenstein, R. (Eds.). (2010). *Mathematics Curriculum: Issues, trends, and future directions* (72nd yearbook of the National Council of Teachers of Mathematics). Reston, VA: NCTM.
- Schmidt, W. H. & et al. (1997). *Many visions, many aims (vol. 1): A cross-national investigation of curriculum in school mathematics*. Kluwer.
- Seah, W. T. & Bishop, A. J. (2002). Values, Mathematics and Society: Making the Connections. Valuing mathematics in society, (105-113), Mathematical Association of Victoria.
- Shimizu, Y., Vithal, R., Ruiz, A., Cuoco, A., Bosch, M., Gholamazad, S., Morony, W., Zhu, Y., & Arzarello, F. (2017). *School mathematics curriculum reforms: challenges, changes and opportunities*. ICMI Study 24. International Commission on Mathematical Instruction
- Stacey. K. (2012). The International Assessment of Mathematical literacy: PISA 2012 Framework and Items. Proceeding of the 12th International Congress on Mathematical Education. Seoul, Korea.
- Supreme Council of Education. (2011). *Theoretical foundations of fundamental change in the formal education of the Islamic Republic of Iran*. Ministry of Education. Iran. (In Farsi.)
- Supreme Council of the Cultural Revolution. (2011). *The Document of fundamental change of education*. Ministry of Education. Iran. (In Farsi.)
- Supreme Council of Education. (2011). *National Curriculum of the Islamic Republic of Iran*. Ministry of Education. Iran. (In Farsi.)

The Effect of Flipped Classroom Teaching Method on Mathematics Learning of 7th Grade Female Students

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Extended Abstract

Introduction

Flipped classroom is a new educational approach in which instructional content are available to students via the Internet, teacher made videos or other visual media, outside the traditional classroom space. Usually students learn mathematical content at home, Library, etc. and then they will participate in the classroom and continue their deep understanding with the guidance of a teacher. They discuss about the topic and its application together with their peers and do the homework through group work at classroom. Since in this approach the typical lecture and homework are reversed, it is called as flipped classroom.

Purpose

The present study aimed to evaluate the effect of flipped classroom approach in teaching and learning mathematics in grade seven at “exponentiation and square root” content.

Methodology

This study was performed in eight sessions (90 minutes) for the topic of “exponentiation and square root” from the mathematics textbook, with the participation of 60 girl students in the Seventh grade. The statistical population of this study was 7th grade girl students in the

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center of one of the southeastern provinces of Iran, which was 2543. Sampling method in this research was randomized sampling. These 60 students were divided into two groups: “experimental” and “control” group. Student in experimental group learn mathematics content related to “exponentiation and square root” with flipped classroom method and control group students learn same math content with traditional teaching method. All students in both groups were participated in final exam with same mathematical content. Experimental group students complete a questionnaire at end of course which ask about students affects about flipped classroom approach. For analyzing the scores of the two groups, co-variance analysis was used.

Results

The results of this study showed that the flipped classroom approach is effective on students' learning progress but the differences in the average for the two different groups are not statistically meaningful. In addition by reviewing the feedback of the students who had participated in the flipped classroom, through the questionnaire and with the help of descriptive statistics, it was found that flipped classroom is encouraging for most of students. Indeed, more than seventy percent of students in experimental group reported that learning mathematics through flipped classroom approach was more enjoyable than the traditional teaching approach. Furthermore, more than eighty percent of students in experimental group revealed that if they have new chance for choosing flipped classroom approach in next school year, then they choose flipped classroom approach.

Discussion

The results of the analysis of students' answers to the questionnaire showed that most of them believe that learning through flipped classroom approach was very effective in improving their learning, because they could watch instructional videos several times and keep the videos when some of the math concepts needed more practice. While in the traditional approach, this was not possible for them. In the flipped classroom approach, students are engaged in the process of learning and discovering concepts actively. In other word, students

were more active and dynamic in flipped classroom approach than in the traditional classroom.

Key words: Flipped Classroom Approach, Traditional Teaching Approach, Mathematical Learning, Constructive Interaction.

References

- Chung, C.J. (2015). Students' Attitudes, Perceptions, and Engagement within a Flipped classroom model as Related to Learning Mathematics. *Journal of Studies in Education*. Vol. 5, No. 3.
- Esmailifar, M. Taghvaie YAzdi, M. Niazazari, K. (1394). Impact of flipped classroom on feeling to belong to the school between primary school students, *National Conference of art studies and humanities researches*. Tehran: Iran. (In Farsi)
- Golzari, Z. & Ataran, M. (1395). Teaching with flipped classroom method in higher education: Narrative of a university lecturer. *Bi-quarterly Journal of theory and practice in curriculum*. 4 (7), 81-136. (In Farsi)
- Gooya, Z. (1393). Transformed meaning of "Educational aid" in the age of information and communication technology. *Roshd Mathematics Educational Journal*. 30(1), 2-3. (In Farsi.)
- Hamdan, N., McKnight, P., McKnight, K., & Arfstrom, K. M. (2013). *A review of flipped learning*. *Flipped Learning Network*. Retrieved from http://www.flippedlearning.org/cms/lib07/VA01923112/Centricity/Domain/41/LitReview_FlippedLearning.pdf by May 2020.
- Hergenbahn, B. R. & Olson, M. R. (2005). *An introduction to theories of learning*. Translated by Aliakbar Seif, (1388). Tehran: Doran Publisher. (In Farsi.)
- Ingram, D., Wiley, B., Miller, C. & Wyberg, T. (2014). *A Study of the Flipped Math Classroom in the Elementary Grades*. Unpublished PhD Dissertation, University of Minnesota, College of Education and Human Development, Center for Applied Research and Educational Improvement.
- Kaviani, H., Liaghatdar, M., Zamani, B. Abedini, Y. (1396a). Flipped classroom theoretical framework: Draw hint for students' center learning. *Foundation of Education*. 7(2), 59-78. (In Farsi.)



- Kaviani, H., Liaghatdar, M., Zamani, B. Abedini, Y. (1396b). The Learning Process in the Flipped Classroom: A Representation of Experienced Curriculum in Higher Education. *Journal of Higher Education Curriculum Studies*, 8(15), 179 -214. (In Farsi.)
- Kheirabadi, R. (1396). Impact of flipped classroom approach in learning of English grammar at grade 10. *Educational Innovation Journal*, 16(64), 141-162. (In Farsi.)
- Louw, J., Muller, J., & Tredoux, C. (2008). Time-on-task, technology and mathematics achievement. *Evaluation and Program Planning*, 31(1), 41-50.
- Kiahasani, Z. & Dosti, V. (1394). Comparison of effect of flipped classroom teaching and traditional teaching method on math learning between grade 5 primary students. *4th International Conference on Psychology and Social Science*. Tehran, Iran. (In Farsi.)
- Mansob Basiri, A. (1394). Kelas: the cure for any flipped pain. *Monthly Teacher Roshd Magazine*. 289 (Special Issue), 10-11. (In Farsi.)
- Mc Callum, S., Schultz, J., Sellke, K., Spartz, J. (2015). An Examination of the Flipped Classroom Approach on College Student Academic Involvement”, *International Journal of Teaching and Learning in Higher Education*. Vol. 27, No. 1, pp. 42-45.
- Nouri, J. (2016). The flipped classroom: for active, effective and increased learning- especially for low achievers. *International Journal of Educational Technology in Higher Education*. 13(33). <https://doi.org/10.1186/s41239-016-0032-z>
- Ollerton, M. (2014). *Differentiation in mathematics classrooms. Mathematics Teaching*. Retrieved from <http://www.atm.org.uk/Mathematics-Teaching-Journal-Archive/15344>, by May 2020.
- Papic, A. (2011). Factors influencing the innovative use of information and communication technology in education by high school teachers. *Information Technology Interfaces (ITI), Proceedings of the ITI 2011 33rd International Conference on Technology in Education* (pp. 313, 318). Osijek, Croatia: Department of Informational Science.

- Rafiepour, A. & Gooya, Z. (2004). Seven Situations to assimilate ICT in Mathematics Education. Printed in selected article of 7th *Iranian Mathematics Education Conference*. Sanandaj, Iran. Pp 79-90. (In Farsi.)
- Saunders, J. M. (2014). *The Flipped Classroom: It's Effect on Student Academic Achievement and Thinking Skills in High School Mathematics*. Unpublished Ph.D. dissertation, Liberty University.
- Shafique, M & Irwin-Robinson, H. (2015). A Study on the Effectiveness of Flipped Teaching in College Math Classroom. *International Journal of Education and Information Technology*. 1(2), 20-33.
- Slavin, R. V. (2006). *Educational Psychology (Theory and Practice)*. Translated by Yahya Seied Mohamadi, (1393). Tehran: Ravan publisher. (In Farsi.)
- Strohmyer, D. (2016). *Student Perception of Flipped Learning in a High School Math Classroom*. Unpublished Ph.D. dissertation, Walden University.
- Waserman, N. H., Quint, C., Norris, S. A., Carr, T. (2017). Exploring Flipped Classroom Instruction in Calculus III. *International Journal of Science and Mathematics Education*. Vol. 15:545–568.
- Zhang, H. W., Du, X. M., Yuan, X. F., & Zhang, L. M. (2016). The Effectiveness of the Flipped Classroom Mode on the English Pronunciation Course. *Creative Education*. 7, 1340-1346. Retrieved from <http://dx.doi.org/10.4236/ce.2016.79139b> by May 2020.



Teachers' Perspective of how High School Mathematics is influenced by University Mathematics

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Extended Abstract

Introduction

In the beginning of the 20th century, Felix Kline wrote a book titled “Elementary Mathematics from a Higher (Advanced) Standpoint” for school teachers to enhance their mathematical knowledge suitable for teaching. More than a century has passed and still, there is even a bigger argument about the nature of mathematical knowledge that high school teachers need to teach.

Purpose

In last three decades, there has been a growing body of research findings in the field of mathematics teacher education, regarding different kinds of mathematics knowledge necessary to prospective secondary teachers' preparation. However, in recent years, a new construct called “School- Related Content Knowledge: SRCK” has been introduced to the field; a unique kind of knowledge that is content- based to make connection between academic/ university mathematics and mathematics that is taught at high school. This knowledge is mathematical in nature and its purpose is to legitimize school mathematics and change the academic subject into a more suitable school subject to better understand the relation between university and school mathematics, a study was designed and conducted with 19 upper secondary mathematics teachers

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Methodology

To conduct the research, qualitative methodology and in specific, grounded theory and narrative method was used. The data collected from four different sources to ensure the validity of the findings using triangulation technique. The data collected via educational and teaching background of the participants to better understand their university and school mathematics experiences, semi- constructed individual interviews with 12 questions, written interviews with five mathematics problems and first author's class observations and field notes.

Analysis

By systematic reduction of the data, two categories emerged with of a number of sub-categories. The first category labeled as “the ways in which, teachers use academic mathematics in their high school teaching” with five sub-categories as “direct use in teaching”, “to make example or contra- example”, “when encounter with problems that there is no classic answer to them”, “to give a holistic view about the nature of mathematics and university and school mathematics” and “to prepare for answering unexpected questions from students”. The second category shaped as “the gap between academic vs. high school mathematics” and included three sub-categories labeled as “the lack of holistic view towards student- teachers at secondary level”, “the unfamiliarity with real- word problems” and “the lack of consistency between different mathematics teacher training programs” in Iran that its education system including curriculum and assessment, is centralized.

Conclusion

The study concluded that for enhancement of the mathematics teacher education program in Iran, it is important to design specific mathematics courses that are content- based, different from both mathematics and all kinds of pedagogical courses that their main responsibility is to help prospective high school teachers to re-tailoring academic mathematics to better serve the purpose of high school mathematics.



Key words: University Mathematics, School Mathematics, High School Teachers, School- Related Content Knowledge.

References

- Association of Mathematics Teacher Educators. (2017). *Standards for preparing teachers of mathematics*. Available online at amte.net/standards.
- Association of Mathematics Teacher Educators. (2020). *Standards for preparing teachers of mathematics*. Information Age Publishing Inc and & the Association of Mathematics Teacher Educators.
- Ball, D. & Bass, H. (2003). Toward a practice-based theory of mathematical knowledge for teaching. In B. Davis and E. Simmt (Eds.); *Proceedings of the 2002 annual meeting of the Canadian Mathematics Education Study Group*; 3-14.
- Ball, D. (2000). Bridging Practices: Intertwining content and pedagogy in teaching and learning to teach. *Journal of Teacher Education*; 51(3), 241-247. Springer.
- Ball, D., Thames, M. & Phelps, G. (2008). Content knowledge for teacher: What makes it special? *Journal of Teacher Education*; 59(5), 389-407. Springer.
- Bromme, R. (1994). Beyond subject matter: A psychological topology of teachers' professional knowledge. In R. Biehler; R.W. Scholz; R. Straesser & B. Winkelmann. (Eds.); *Mathematics didactics as a scientific discipline: The state of the art*; pp. 73–88. Kluwer Academic Publishers.
- Burns, M. (2014). Uncovering the Math Curriculum. Educational Leadership. Translated by S. Gholamazad. 12-16. *Roshd Mathematics Education Journal*. No. 122. 12-16. Publishing & Teaching Technology Office, Organization for Educational Planning, Ministry of Education, Iran. (In Farsi.)
- Conference Board of the Mathematical Sciences (CBMS). (2012). *The mathematical education of teachers II*. Providence, RI: American Mathematical Society.
- Dreher, A., Lindmeier, A., Heinze, A., & Niemand, C. (2018). What kind of content knowledge do secondary mathematics teachers need? A conceptualization taking into account academic and

- school Mathematics. *Journal of Math Didakt.* 39:319–341. Springer.
- Eichler, A. & Ernes, R. (2014). Teachers' beliefs towards teaching calculus, *ZDM Mathematics Education.* 46:647–659. Springer.
- Gooya, Z. (2005). The knowledge needed for teaching at elementary school. *Roshd Mathematics Education Journal.* No. 80. 23- 30. Publishing & Teaching Technology Office, Organization for Educational Planning, Ministry of Education, Iran. (In Farsi.)
- Gooya, Z.; & Mortazi Mehrabani, N. (2014). Final Report of the Research Project: The knowledge that teachers need to teach mathematics at elementary schools. Research Center for Curriculum & Educational Innovations. Ministry of Education. (In Farsi.)
- Hill, H., Rowan, B. & Ball, D. (2005). Effects of Teachers' Mathematical Knowledge for Teaching on Student Achievement. *American Educational Research Journal.* Vol. 42, No. 2, pp. 371–406
- Hodge, A., Gerberry, C., Moss, E., & Staples, E. (2010). Purposes and Perceptions: What do university mathematics professors see as their role in the education of secondary mathematics teachers? *PRIMUS.* 20 (8), 646-663. Taylor & Francis Group.
- Lincoln, Y. S. & Guba, E. G. (1985). *Naturalistic enquiry.* Sage Publishing.
- Ma, L. P. (1999). Knowing and teaching elementary mathematics: Teachers' understanding of fundamental mathematics in China and the United States. *Educational Studies in Mathematics.* 42, 101-106. Springer.
- McCrary, R., Floden, R., Ferrini-Mundy, J., Reckase, M. & Senk, S. (2012). Knowledge of Algebra for Teaching: A Framework of Knowledge and Practices. *Journal for Research in Mathematics Education.* Vol. 43, No. 5, pp. 584-615. National Council of Teachers of Mathematics.
- National Council of Teachers of Mathematics: NCTM. (1991). *Professional Standards for Teaching Mathematics.* Reston, VA. The Author.
- Nezhad Irad Mousa, M. (2017). Rosh Mathematics Borhan Journal. No. 98. 19-20. Publishing & Teaching Technology Office,



- Organization for Educational Planning, Ministry of Education, Iran. (In Farsi.)
- Shulman, L. (1986). Those who understand: Knowledge growth in teaching. *Educational Researcher*. 15(2), 4–14. American Educational Research Association.
- Speer, N., King, K. & Howell, H. (2015). Definitions of mathematical knowledge for teaching: Using these constructs in research on secondary and college mathematics teachers. *Journal of Mathematics Teacher Education*. 18(2), 105–122. Springer.
- Stylianides, G. J. & Stylianides, A. J. (2010). Mathematics for teaching: A form of applied mathematics. *Journal teaching and teacher education*. 26: 161–172. Elsevier Ltd.
- Turner, F. & Rowland, T. (2011). The knowledge quartet as an organizing framework for developing and deepening teachers' mathematics knowledge. From Book *Mathematical knowledge in teaching*, 195-211.
- Weigand, H., McCallum, W., Menghini, M., Neubrand, M., Schubring, G. & Tobies, T. (2017). What is and what might be the legacy of Felix Klein? *Proceedings of ICMI13 in Hamburg*. 321-334. Springer.
- Wu, H. (2011). The mis-education of mathematics teachers. *Notices of the AMS*. Vol. 58, N. 3, pp 372-382. American Mathematical Society.
- Zazkis, R. & Leikin, R. (2010). Advanced mathematical knowledge in teaching practice: Perceptions of secondary mathematics teachers. *Mathematical Thinking and Learning*. 12:263-281 .Taylor & Francis Group.
- Zazkis, R., Leikin, R. & Meller, M. (2017). Research mathematicians as teacher educators: Focusing on mathematics for secondary mathematics teachers. *Journal of Mathematics Teacher Education*. Springer.

Critical Review of Studies in the Field of Mathematical Word Problems

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Extended Abstract

Introduction

Mathematics plays an important role in empowering people to live and work in extremely complicated world. Thus in almost all formal educational systems, mathematics is essential school subject matter. Numerous researchers believe that mathematical word problems are effective in enhancing students' mathematical knowledge and their problem solving skills and enabling them to apply mathematics in solving daily life problems. Because of the importance of word problems, a considerable number of research have been conducted in Iran within the recent decade 2009- 2019.)

Purpose

The purpose of the present study was to evaluate the research methodologies used by researches conducted in the field of mathematical word problems in Iran to help mathematics education researchers to learn from what have been done and choose their future direction more realistically.

Methodology

In doing so, major relevant Iranian data bases including Iran doc, Sid, Google Scholar, Noor, Civilica, Magiran, central library database of Farhangian university, Ferdosi university of Mashhad, University of Tehran, Shahid Beheshti University and Elmnet, were reviewed and searched and 136 studies were identified. By taking one decade time

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interval of 2009 to 2019 and using “verbal problem” or “mathematical verbal problem” as keyword in research reports’ title, 19 studies in the field of word problem were identified. In the next step, these reports were evaluated by using critical review research method.

Results

The results showed that the majority of these 19 researches, used quantitative methodology. In addition, most of them dealt with student’s challenges in solving word problems. Some of the researches involved the effects of new teaching methods on solving word problems. A number of researches discussed the role of cognitive – metacognitive and emotional factors on students’ word problem solving performance. Furthermore, investigating neurological factors and linguistic abilities in solving word problems were another focal point some of the researches that carried on in this field. In the next step, descriptive information of selected researches consisted of research questions, research methods, characteristics of participants and the way they have been selected, data collecting tools, technical reports of instruments, structure of mathematical problems and the data analysis methods were critically reviewed.

Discussion

In reviewing research methodologies of 19 research reports in the field of mathematical word problems, the improper statement of research questions and inconsistency between the type of research method and research questions were salient. In addition, many other research component including incomplete use of “statistical population”, insufficient report on the method of determining the sample size, failure to report technical characteristics of measurement tools, ignoring exploratory analysis of the data, failure to refer to the assumptions of statistical models and insufficiency to report evidence of the data, threatened the validity of those research studies. The concluding remark is that it is necessary to make sure that the research approach is relevant and consistent with the nature of research purpose and research questions. Also, in taking either quantitative or qualitative approaches to research, every measure should be taken to assure the precision and validation of research process. Only in this case, the findings could be trusted and validated and reliable.

Key Words: Mathematical Word Problems, Critical Review, Research Methodology.

References

- Afshinmanesh, M. (2012). *An Investigation of the effect of drawing-based teaching on algebraic modeling of word problems in 7th Grade male students*. Unpublished Master Thesis in Mathematics Education. Tarbiat Dabir Shahid Rajaei University. (In Farsi.)
- Ahadpour, E. (2017). *The Analysis of Mistakes of Girl and Boy Students in 8th Grade, while Solving Word Problems of Linear Equations Based on Newman's Model*. Unpublished Master Thesis in Mathematics Education. Farhangian University. (In Farsi.)
- Aminifar, E; Alamolhodaei, H; & Abdullahi, S. H. (2012). The role of mathematical anxiety and students' learning styles in solving verbal problems in arithmetic. *Quarterly Journal of Educational Innovations*. 11(42), 105-118. (In Farsi.)
- Asadnejad Proj, S. (2016). *The investigation of 4th Grade students' ability on word problem solving based on the Newman's Error Analysis model*. Unpublished Master Thesis in Mathematics Education. Farhangian University. (In Farsi.)
- Bakhtiari, M. (2012). *The comparison of verbal-psychological abilities of the strong and weak elementary 3rd Grade girls in solving mathematics word problems*. Unpublished Master Thesis in Mathematics Education. Payame Noor Center, Tehran. (In Farsi.)
- Azizi Mahmoodabad, M; Liaghatdar, M. J; & Oreyzi, H. R. (2019). Investigating the effectiveness of illustration representation-based Instruction on word problem-solving ability in mathematics. *Research in Curriculum Planning*. 9(2), 200-224. (In Farsi.)
- Baloğlu, M.; & Koçak, R. (2006). A multivariate investigation of the differences in mathematics anxiety. *Personality and Individual Differences*. 40(7), 1325-1335.
- Bargi, M. (2013). *A study on the role of cognitive style in applying metacognitive strategies in solving mathematical word problems*. Unpublished Master Thesis in Mathematics Education. Mashhad Ferdowsi University. (In Farsi.)
- Faizy, A. (2016). *Assessing the understanding and comprehension of math verbal problems of bilingual high school students*. Unpublished Master Thesis in Mathematics Education. Shahid Beheshti University. (In Farsi.)



- Gall, M; Borg, W; & Gall, J. (1996). *Quantitative and qualitative research methods in educational sciences and psychology*. Translated by Ahmad Reza Nasr et al. Tehran: Samt Publications. (In Farsi.)
- Ghadami, S. (2013). *Assessing the performance of first grade high school students in solving verbal problems*. Unpublished Master Thesis in Mathematics Education. Shahid Beheshti University. (In Farsi.)
- Grant, M. J. & Booth, A. (2009). A typology of reviews: an analysis of 14 review types and associated methodologies, *Health Information and Libraries Journal*. 26, 91–108.
- Greer, B.; Verschaffel, L.; & Mukhopadhyay, S. (2007). Modelling for life: Mathematics and children's experience. In *Modelling and applications in mathematics education* (pp. 89–98). Springer.
- Haghverdi, M. (2014). The characteristics of mathematical word problems at the middle school and suggested strategies to facilitate their solution process. *Journal of Theory & Practice in Curriculum*, 2(3), 25-46. (In Farsi.)
- Haghverdi, M; Shahorani Semnani, A; & Seifi, M. (2011). Identify and classify the types of mistakes students make in solving math verbal problems. *Journal of Applied Mathematics, Lahijan Branch, Azad University*. Vol 8, No 3 (continues 30), 1-9. (In Farsi.)
- Johnson, R. B; Christensen, L. (2014). *Educational Research Quantitative, Qualitative, and Mixed Approaches*. Translated by Kiamanesh, Esmaili, Hassanvandi, Danae Toos, Fathi and Mohsenpour. Tehran: Elm Publishing. (In Farsi.)
- Karimi, F; Moradi, A; Kadivar, P; & Karaminoori, R. (2015). Predicting students' performance in solving math verbal problems with respect to cognitive, metacognitive and emotional variables. *Education Quarterly*, 31(1), 9-44. (In Farsi.)
- Karimi, F; Moradi, A; Kadivar, P; & Karaminoori, R. (2012). Factor analysis of metacognitive monitoring test for solving mathematical verbal problems. *Journal of Psychological Sciences*, 11(44), 7-24. (In Farsi.)
- Khani Basiri, L. (2017). *The effect of manipulation on reducing the errors of elementary fourth grade students in solving the verbal problems of fractions based on the Newman error analysis model*. Unpublished Master Thesis in Mathematics Education. Farhangian University. (In Farsi.)
- Kiamanesh, A; Mohsenpour, M; Safarkhani, M; & Aghdasi, S. (2012). The trend of changes in the mathematical performance of third grade

- middle school students in the period of 1999-2007 based on the findings of TIMSS international studies in Iran and the countries of the region according to the objectives of the 20-year vision document. *Iranian Curriculum Studies Quarterly*, 24(6), 59-82. (In Farsi.)
- Kilpatrick, J; Swafford, J. (2003). Helping children learn mathematics. Translated by Mahdi Behzad and Zahra Gooya. Tehran: Fatemi Publications. (In Farsi.)
- Mohsenpour, M; Gooya, Z; Shokouhi Yekta, M; Kiamanesh, A, R. & Bazargan, A. (2015). Diagnostic test of cognitive competence of mathematical literacy based on Pisa cognitive model. *Quarterly Journal of Educational Innovations*. 14(1), 7-33. (In Farsi.)
- Perihan, D. A. (2015). Preschool childrens skills in solving mathematical word problems. *Educational Research and Reviews*, 10(18), 2539–2549. <https://doi.org/10.5897/err2015.2431>
- Reed, S. K. (1999). *Word problems: Research and curriculum reform*. Routledge.
- Roobahani, SH; Hassanabadi, H. R. (2015). Central Executive Function and Phonological Loop in Students with Mathematical Word Problems Solving Disability. *Exceptional Children Quarterly*, 15(4), 5-20. (In Farsi.)
- Saberi, M. (2018). *Analysis the errors of the 12th Graders' "Natural Science Branch" in solving word problems of application of derivative based on Newman's Error Analysis Model in City of Semirom*. Unpublished Master Thesis in Mathematics Education. Farhangian University. (In Farsi.)
- Salimi, M; Sadi pour, E; Delavar, A; & Maleki, H. (2014). Comparison of training effects in imagery strategies of mental imagery of think-aloud of written representation and motor representation on the performance of elementary students in solving verbal math problems. *Research in Curriculum Planning*, Vol 11, No 14 (continues 41), 12-22. (In Farsi.)
- Sarmad, Z; Bazargan, A; & Hejazi, E. (2015). *Research Methods in Behavioral Sciences*. Tehran: Agah Publication. (In Farsi.)
- Santos-trigo, M.; & Gooya, Z. (2015). Mathematical Problem Solving. *The Proceedings of the 12th International Congress on Mathematical Education*, 459–462.
- Shahmoradi, F. (2018). *Identifying the type of errors of 7th Grade Students in Tehran's Education District 15 in mathematical word problems*. Unpublished Master Thesis in Mathematics Education. Farhangian University. (In Farsi.)
- Verschaffel, L.; Greer, B.; & De



Corte, E. (2000). *Making sense of word problems*. Swets & Zeitlinger Lisse.

Vicente, S.; Orrantia, J.; & Verschaffel, L. (2007). Influence of situational and conceptual rewording on word problem solving. *British Journal of Educational Psychology*, 77(4), 829–848.

Wong, W.-K.; Hsu, S. C.; Wu, S. H.; Lee, C. W.; & Hsu, W. L. (2007). LIM-G: Learner-initiating instruction model based on cognitive knowledge for geometry word problem comprehension. *Computers & Education*, 48(4), 582–601.